Package ‘neldermead’
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Description Provides several direct search optimization algorithms based on the simplex method. The provided algorithms are direct search algorithms, i.e. algorithms which do not use the derivative of the cost function. They are based on the update of a simplex. The following algorithms are available: the fixed shape simplex method of Spendley, Hext and Himsworth (unconstrained optimization with a fixed shape simplex), the variable shape simplex method of Nelder and Mead (unconstrained optimization with a variable shape simplex made), and Box’s complex method (constrained optimization with a variable shape simplex).
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Description

The goal of this package is to provide a Nelder-Mead direct search optimization method. That Nelder-Mead algorithm may be used in the following optimization context:

- there is no need to provide the derivatives of the objective function,
- the number of parameters is small (up to 10-20),
- there are bounds and/or non linear constraints.

Design

This package provides the following components:

- **neldermead** provides various Nelder-Mead variants and manages for Nelder-Mead specific settings, such as the method to compute the initial simplex, the specific termination criteria,
- **fminsearch** provides a simplified Nelder-Mead algorithm. Specific termination criteria, initial simplex and auxiliary settings are automatically configured.
- **fminbnd** provides a simplified Box algorithm, i.e. the equivalent of **fminsearch** for unconstrained search.
- **optimset**, **optimget** provide commands to emulate their Scilab counterparts.
- **optimplotfunccount**, **optimplotx** and **optimplotfval** provide plotting features for the **fminsearch** function (Not implemented yet).
- **nmplot** provides a high-level component which provides directly output pictures for Nelder-Mead algorithm. (Not implemented yet).

The current component is based on the following packages
• **optimbase**: provides an abstract class for a general optimization component, including the number of variables, the minimum and maximum bounds, the number of non linear inequality constraints, the logging system, various termination criteria, the cost function, etc...

• **optimsimplex**: provides a class to manage a simplex made of an arbitrary number of vertices, including the computation of a simplex by various methods (axes, regular, Pfeffer’s, randomized bounds), the computation of the size by various methods (diameter, sigma+, sigma-, etc...).

### Features

The following is a list of features the Nelder-Mead prototype algorithm currently provides:

• Provides 3 algorithms, including
  – the fixed shape algorithm of Spendley et al.,
  – the variable shape algorithm of Nelder and Mead,
  – Box’s ‘complex’ algorithm managing bounds and nonlinear inequality constraints based on arbitrary number of vertices in the simplex.

• Manage various simplex initializations:
  – initial simplex given by user,
  – initial simplex computed with a length and along the coordinate axes,
  – initial regular simplex computed with formula of Spendley et al.,
  – initial simplex computed by a small perturbation around the initial guess point.

• Manage cost function:
  – optional additional argument,
  – direct communication of the task to perform: cost function or inequality constraints.

• Manage various termination criteria, including maximum number of iterations, tolerance on function value (relative or absolute):
  – tolerance on x (relative or absolute),
  – tolerance on standard deviation of function value (original termination criteria in Box 1965),
  – maximum number of evaluations of cost function,
  – absolute or relative simplex size.

• Manage the history of the convergence, including:
  – history of function values,
  – history of optimum point,
  – history of simplices,
  – history of termination criteria.

• Provide a plot command which allows to graphically see the history of the simplices toward the optimum (Not yet implemented).

• Provide query features for the status of the optimization process: number of iterations, number of function evaluations, status of execution, function value at initial point, function value at optimal point, etc...

• Kelley restart based on simplex gradient.

• O’Neill restart based on factorial search around optimum.

### Details
See vignette('neldermead',package='neldermead') for more information.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

References


'Detection and Remediation of Stagnation in the Nelder–Mead Algorithm Using a Sufficient Decrease Condition’, Kelley C. T., SIAM J. on Optimization, 1999


See Also

optimbase optimsimplex

---

costf.transposex Cost Function Call

Description

Call the cost function after transposition of the value of the point estimate x, so that the input row vector, given by optimsimplex, is transposed into a column vector as required by the cost function.
Usage

costf.transpose(x = NULL, this = NULL)

Arguments

x The point estimate provide as a row matrix.
this A neldermead object.

Value

Return the value of the cost function (called by neldermead.costf.)

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

neldermead.costf

Description

Evaluate an unconstrained cost function on a grid of points around a given initial point estimate.

Usage

fmin.gridsearch(fun = NULL, x0 = NULL, xmin = NULL, xmax = NULL, npts = 3, alpha = 10)

Arguments

fun An unconstrained cost function returning a numeric scalar, similar to those used in the fminsearch function.
x0 The initial point estimate, provided as a numeric vector.
xmin Optional: a vector of lower bounds.
xmax Optional: a vector of upper bounds.
npts An integer scalar greater than 2, indicating the number of evaluation points will be used on each dimension to build the search grid.
alpha A vector of numbers greater than 1, which give the factor(s) used to calculate the evaluation range of each dimension of the search grid (see Details). If alpha length is lower than that of x0, elements of alpha are recycled. If its length is higher than that of x0, alpha is truncated.
Details

fminbnd evaluates the cost function at each point of a grid of npts*length(x0) points. If lower (xmin) and upper (xmax) bounds are provided, the range of evaluation points is limited by those bounds and alpha is not used. Otherwise, the range of evaluation points is defined as [x0/alpha,x0*alpha].

The actual evaluation of the cost function is delegated to optimbase.gridsearch.

Value

Return a data.frame with the coordinates of the evaluation point, the value of the cost function and its feasibility. Because the cost function is unconstrained, it is always feasible. The data.frame is ordered by feasibility and increasing value of the cost function.

Author(s)

Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

fminsearch, optimbase.gridsearch

Description

EXPERIMENTAL.

This function searches for the constrained minimum of a given cost function. The provided algorithm is a direct search algorithm, i.e. an algorithm which does not use the derivative of the cost function. It is based on the update of a simplex, which is a set of k>=n+1 vertices, where each vertex is associated with one point, which coordinates are constrained within user-defined boundaries, and with one function value. This algorithm corresponds to a version of the Box algorithm, based on bounds and no non-linear constraints. This function is based on a specialized use of the more general neldermead function bundle. Users who want to have a more flexible solution based on direct search algorithms should consider using the neldermead functions instead of the fminbnd function.

Usage

fminbnd(fun=NULL, x0=NULL, xmin=NULL, xmax=NULL, options=NULL, verbose=FALSE)
Arguments

- **fun**: A cost function return a numeric scalar.
- **x0**: A numerical vector of initial guesses (length n).
- **xmin**: A numerical vector of lower bounds for x0 (length n).
- **xmax**: A numerical vector of upper bounds for x0 (length n).
- **options**: A list of optimization options, which drives the behaviour of fminbnd. These options must be set with the optimset function (see ?optimset) which returns a list with the following elements:
  - **MaxIter**: The maximum number of iterations. The default is 200 * n.
  - **MaxFunEvals**: The maximum number of evaluations of the cost function. The default is 200 * n.
  - **BoxTolFun**: The absolute tolerance on function value. The default value is 1.e-4.
  - **TolFun**: The absolute tolerance on function value. The default value is 1.e-4.
  - **TolX**: The absolute tolerance on simplex size. The default value is 1.e-4.
  - **Display**: The verbose level.
  - **OutputFcn**: The output function, or a list of output functions called at the end of each iteration. The default value is NULL.
  - **PlotFcns**: The plot function, or a list of plotput functions called at the end of each iteration. The default value is empty.
- **verbose**: The verbose option, controlling the amount of messages.

Details

Termination criteria

In this section, we describe the termination criteria used by fminbnd. The criteria is based on the following variables:

- **boxkount**: the current number of time the tolerance on the cost function was met, and
- **shiftfv**: the absolute value of the difference of function value between the highest and lowest vertices.

If both \( \text{shiftfv} < \text{options$TolFun} \) and \( \text{boxkount} < \text{options$nbMatch} \) conditions are true, then the iterations stop.

The initial simplex

The fminbnd algorithm uses a special initial simplex, which is an heuristic depending on the initial guess. The strategy chosen by fminbnd corresponds to the content of simplex$method element of the neldermead object (set to 'randbounds'). It is applied using the content of the bounds$min and bounds$min elements to generate a simplex with random vertices within the boundaries defined by the user (ie, xmin, and xmax). This method is an heuristic which is presented in ‘A New Method of Constrained Optimization and a Comparison With Other Methods’ by M.J. Box. See in the help of optim simplex for more details.

The number of iterations

In this section, we present the default values for the number of iterations in fminbnd.
The options input argument is an optional list which can contain the MaxIter field, which stores the maximum number of iterations. The default value is 200n, where n is the number of variables. The factor 200 has not been chosen by chance, but is the result of experiments performed against quadratic functions with increasing space dimension. This result is presented in "Effect of dimensionality on the Nelder-Mead simplex method" by Lixing Han and Michael Neumann. This paper is based on Lixing Han's PhD, 'Algorithms in Unconstrained Optimization'. The study is based on numerical experiments with a quadratic function where the number of terms depends on the dimension of the space (i.e. the number of variables). Their study showed that the number of iterations required to reach the tolerance criteria is roughly 100n. Most iterations are based on inside contractions. Since each step of the Nelder-Mead algorithm only require one or two function evaluations, the number of required function evaluations in this experiment is also roughly 100n.

Output and plot functions

The optimset function can be used to configure one or more output and plot functions. The output or plot function is expected to have the following definition:

```r
myfun <- function(x, optimValues, state)
```

The input arguments x, optimValues and state are described in detail in the optimset help page. The optimValues$procedure field represents the type of step performed at the current iteration and can be equal to one of the following strings:

- " (the empty string),
- 'initial simplex',
- 'reflect (Box)'.

Value

Return a object of class neldermead. Use the neldermead.get to extract the following element from the returned object:

- **xopt** The vector of n numeric values, minimizing the cost function.
- **fopt** The minimum value of the cost function.
- **exitflag** The flag associated with exist status of the algorithm. The following values are available:
  - -1 The maximum number of iterations has been reached.
  - 0 The maximum number of function evaluations has been reached.
  - 1 The tolerance on the simplex size and function value delta has been reached. This signifies that the algorithm has converged, probably to a solution of the problem.
- **output** A list which stores detailed information about the exit of the algorithm. This list contains the following fields:
  - **algorithm** A string containing the definition of the algorithm used, i.e. 'Nelder-Mead simplex direct search'.
  - **funcCount** The number of function evaluations.
  - **iterations** The number of iterations.
  - **message** A string containing a termination message.

Author(s)

Author: Sebastien Bihorel (<sb.pmlab@gmail.com>)
See Also

optimset

Examples

In the following example, we use the fminbnd function to compute the minimum
of a quadratic function. We first define the function 'quad', and then use
the fminbnd function to search the minimum, starting with the initial guess
(1.2, 1.9) and bounds of (1, 1) and (2, 2). In this particular case, 11
iterations are performed with 20 function evaluations.

```r
quad <- function(x)
  y <- x[1]^2 + x[2]^2

sol <- fminbnd(quad, c(1.2, 1.9), c(1, 1), c(2, 2))
summary(sol)
```

Description

This function calls the cost function and makes it match neldermead requirements. It is used in
the fminbnd function as the function element of the neldermead object (see ?neldermead and
?neldermead.set).

Usage

```r
fminbnd.function(x = NULL, index = NULL, fmsfundata = NULL)
```

Arguments

- `x` A single column vector of parameter estimates.
- `index` An integer variable set to 2, indicating that only the cost function is to be com-
  puted by the algorithm.
- `fmsfundata` An object of class 'optimbase.functionargs' and with (at least) a
  `fun` element, which contains the user-defined cost function.

Value

Returns a list with the following elements:

- `f` The value of the cost function at the current point estimate.
- `index` The same index variable.
- `this` A list with a single element `costargument` which contains `fmsfundata`. 

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`fminbnd.function`  

`fminbnd Cost Function Call`

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`fminbnd Cost Function Call`
Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

fminbnd, neldermead, neldermead.set.

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**fminbnd.outputfun**

*fminbnd Output Function Call*

**Description**

This function calls the output function and make it match neldermead requirements. It is used in the fminbnd function as the outputcommand element of the neldermead object (see ?neldermead and ?neldermead.set).

**Usage**

```r
fminbnd.outputfun(state = NULL, data = NULL, fmsdata = NULL)
```

**Arguments**

- **state**
  - The current state of the algorithm either 'init', 'iter' or 'done'.

- **data**
  - The data at the current state. This is an object of class 'neldermead.data', i.e. a list with the following elements:
    - **x** The current parameter estimates.
    - **fval** The current value of the cost function.
    - **simplex** The current simplex object.
    - **iteration** The number of iterations performed.
    - **funcount** The number of function evaluations.
    - **step** The type of step in the previous iteration.

- **fmsdata**
  - This is an object of class 'optimbase.functionargs' which contains specific data of the fminbnd algorithm:
    - **Display** what to display
    - **OutputFen** the array of output functions
    - **PlotFcns** the array of plot functions

**Value**

This function does not return any data, but execute the output function(s).
fminsearch

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also
fminbnd, neldermead, neldermead.set.

fminsearch

Computation of the unconstrained minimum of given function with the Nelder-Mead algorithm.

Description
This function searches for the unconstrained minimum of a given cost function. The provided algorithm is a direct search algorithm, i.e. an algorithm which does not use the derivative of the cost function. It is based on the update of a simplex, which is a set of k>=n+1 vertices, where each vertex is associated with one point and one function value. This algorithm is the Nelder-Mead algorithm. This function is based on a specialized use of the more general neldermead function bundle. Users who want to have a more flexible solution based on direct search algorithms should consider using the neldermead functions instead of the fminsearch function.

Usage
fminsearch(fun = NULL, x0 = NULL, options = NULL, verbose=FALSE)

Arguments
fun A cost function return a numeric scalar.
x0 A numerical vector of initial guesses (length n).
options A list of optimization options, which drives the behaviour of fminsearch. These options must be set with the optimset function (see ?optimset) which returns a list with the following elements:
MaxIter The maximum number of iterations. The default is 200 * n.
MaxFunEvals The maximum number of evaluations of the cost function. The default is 200 * n.
TolFun The absolute tolerance on function value. The default value is 1.e-4.
TolX The absolute tolerance on simplex size. The default value is 1.e-4.
Display The verbose level.
OutputFcn The output function, or a list of output functions called at the end of each iteration. The default value is NULL.
PlotFcns The plot function, or a list of plot functions called at the end of each iteration. The default value is empty.
verbose The verbose option, controlling the amount of messages.
Details

Termination criteria
In this section, we describe the termination criteria used by fminsearch. The criteria is based on the following variables:

- \( s_{size} \) the current simplex size,
- \( s_{shiftfv} \) the absolute value of the difference of function value between the highest and lowest vertices.

If both \( s_{size} < \text{options}$TolX \) and \( s_{shiftfv} < \text{options}$TolFun \) conditions are true, then the iterations stop. The size of the simplex is computed using the 'sigmaplus' method of the optim simplex package. The 'sigmamplus' size is the maximum length of the vector from each vertex to the first vertex. It requires one loop over the vertices of the simplex.

The initial simplex
The fminsearch algorithm uses a special initial simplex, which is an heuristic depending on the initial guess. The strategy chosen by fminsearch corresponds to the content of simplex$\text{method}$ element of the neldermead object (set to 'pfeffer'). It is applied using the content of the simplex$\text{deltausual}$ (0.05) and simplex$\text{deltazero}$ (0.0075) elements. Pfeffer's method is an heuristic which is presented in 'Global Optimization Of Lennard-Jones Atomic Clusters' by Ellen Fan. It is due to L. Pfeffer at Stanford. See in the help of optim simplex for more details.

The number of iterations
In this section, we present the default values for the number of iterations in fminsearch.

The options input argument is an optional list which can contain the MaxIter field, which stores the maximum number of iterations. The default value is 200\( n \), where \( n \) is the number of variables. The factor 200 has not been chosen by chance, but is the result of experiments performed against quadratic functions with increasing space dimension. This result is presented in 'Effect of dimensionality on the Nelder-mead simplex method' by Lixing Han and Michael Neumann. This paper is based on Lixing Han's PhD, 'Algorithms in Unconstrained Optimization'. The study is based on numerical experiments with a quadratic function where the number of terms depends on the dimension of the space (i.e. the number of variables). Their study showed that the number of iterations required to reach the tolerance criteria is roughly 100\( n \). Most iterations are based on inside contractions. Since each step of the Nelder-Mead algorithm only require one or two function evaluations, the number of required function evaluations in this experiment is also roughly 100\( n \).

Output and plot functions
The optimset function can be used to configure one or more output and plot functions. The output or plot function is expected to have the following definition:

\[
\text{myfun} \leftarrow \text{function}(x, \text{optimValues}, \text{state})
\]

The input arguments \( x \), \( \text{optimValues} \) and \( \text{state} \) are described in detail in the optimset help page. The \( \text{optimValues}$\text{procedure}$ \) field represents the type of step performed at the current iteration and can be equal to one of the following strings:

- "" (the empty string),
- 'initial simplex',
- 'expand',
- 'reflect',
• 'contract inside',
• 'contract outside'.

Value
Return a object of class neldermead. Use the neldermead.get to extract the following element from the returned object:

xopt  The vector of n numeric values, minimizing the cost function.
fopt  The minimum value of the cost function.
exitflag  The flag associated with exist status of the algorithm. The following values are available:

-1  The maximum number of iterations has been reached.
  0  The maximum number of function evaluations has been reached.
  1  The tolerance on the simplex size and function value delta has been reached. This signifies that the algorithm has converged, probably to a solution of the problem.

output A list which stores detailed information about the exit of the algorithm. This list contains the following fields:
algorithm  A string containing the definition of the algorithm used, i.e. 'Nelder-Mead simplex direct search'.
funcCount  The number of function evaluations.
iterations  The number of iterations.
message  A string containing a termination message.

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

References
See Also

optimset neldermead

Examples

In the following example, we use the fminsearch function to compute the minimum of the Rosenbrock function. We first define the function 'banana', and then use the fminsearch function to search the minimum, starting with the initial guess $(-1.2, 1.0)$. In this particular case, 85 iterations are performed with 159 function evaluations.

```r
banana <- function(x){
  y <- 100*(x[2]-x[1]^2)^2 + (1-x[1])^2
} 
sol <- fminsearch(banana, c(-1.2,1))
sol
```

In the following example, we configure the absolute tolerance on the size of the simplex to a larger value, so that the algorithm performs less iterations. Since the default value of 'TolX' for the fminsearch function is 1.e-4, we decide to use 1.e-2. The optimset function is used to create an optimization option list and the field 'TolX' is set to 1.e-2. The options list is then passed to the fminsearch function as the third input argument. In this particular case, the number of iterations is 70 with 130 function evaluations.

```r
opt <- optimset(TolX=1.e-2)
sol <- fminsearch(banana, c(-1.2,1), opt)
sol
```

In the following example, we want to produce intermediate outputs of the algorithm. We define the outfun function, which takes the current point x as input argument. The function plots the current point into the current graphic window with the plot function. We use the 'OutputFcn' feature of the optimset function and set it to the output function. Then the option list is passed to the fminsearch function. At each iteration, the output function is called back, which creates and update a plot. While this example creates a 2D plot, the user may customized the output function so that it writes a message in the console, write some data into a data file, etc... The user can distinguish between the output function (associated with the 'OutputFcn' option) and the plot function (associated with the 'PlotFcns' option). See the optimset for more details on this feature.

```r
outfun <- function(x, optimValues, state){
  plot(x[1],x[2],xlim=c(-1.5,1.5),ylim=c(-1.5,1.5))
  par(new=TRUE)
}
```

The 'Display' option allows to get some input about the intermediate steps of the algorithm as well as to be warned in case of a convergence problem. In the following example, we present what happens in case of a convergence
Problem. We set the number of iterations to 10, instead of the default 400 iterations. We know that 85 iterations are required to reach the convergence criteria. Therefore, the convergence criteria is not met and the maximum number of iterations is reached.

```
opt <- optimset(MaxIter=10)
sol <- fminsearch(banana, c(-1.2,1), opt)
```

Since the default value of the 'Display' option is 'notify', a message is generated, which warns the user about a possible convergence problem. The previous script produces the following output.

- Exiting: Maximum number of iterations has been exceeded
- Current function value: 4.135598

In the following example, we present how to display intermediate steps used by the algorithm. We simply set the 'Display' option to the 'iter' value. This option allows to see the number of function evaluations, the minimum function value and which type of simplex step is used for the iteration.

```
opt <- optimset(Display='iter')
sol <- fminsearch(banana, c(-1.2,1), opt)
sol
```

### fminsearch.function

**fninsearch Cost Function Call**

**Description**

This function calls the cost function and makes it match neldermead requirements. It is used in the `fminsearch` function as the function element of the neldermead object (see `?neldermead` and `?neldermead.set`).

**Usage**

```
fminsearch.function(x = NULL, index = NULL, fmsfundata = NULL)
```

**Arguments**

- **x**  A single column vector of parameter estimates.
- **index**  An integer variable set to 2, indicating that only the cost function is to be computed by the algorithm.
- **fmsfundata**  An object of class 'optimbase.functionargs' and with (at least) a fun element, which contains the user-defined cost function.

**Value**

Returns a list with the following elements:

- **f**  The value of the cost function at the current point estimate.
index The same index variable.
this A list with a single element costargument which contains fmsfndata.

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also
fminsearch, neldermead, neldermead.set,

fminsearch.outputfun  fminsearch Output Function Call

Description
This function calls the output function and make it match neldermead requirements. It is used in the fminsearch function as the outputcommand element of the neldermead object (see ?neldermead and ?neldermead.set).

Usage
fminsearch.outputfun(state = NULL, data = NULL, fmsdata = NULL)

Arguments
state The current state of the algorithm either 'init', 'iter' or 'done'.
data The data at the current state. This is an object of class 'neldermead.data', i.e. a list with the following elements:
  x The current parameter estimates.
  fval The current value of the cost function.
  simplex The current simplex object.
  iteration The number of iterations performed.
  funccount The number of function evaluations.
  step The type of step in the previous iteration.
fmsdata This is an object of class 'optimbase.functionargs' which contains specific data of the fminsearch algorithm:
  Display what to display
  OutputFcns the array of output functions
  PlotFcns the array of plot functions

Value
This function does not return any data, but execute the output function(s).
Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

fminsearch, neldermead, neldermead.set.

neldermead S3 neldermead object

Description

These functions support the S3 class 'neldermead' and are intended to either create objects of this class or check if an object is of this class.

Usage

neldermead(optbase, method, simplex0, simplex0method,
  simplex0length, simplex0size0, simplex0opt, historysimplex, coords0, rho, chi,
  gamma, sigma, tolfstdeviation, tolfstdeviationmethod, tolsimplexizeabsolute,
  tolsimplexizerelative, tolsimplexizemethod, toldeltafv, tolssizedeltafvmethod,
  simplex0deltausual, simplex0deltazero, restartsimplexmethod, restartmax,
  restarteps, restartstep, restartnb, restartflag, restartdetection,
  kelleystagnationflag, kelleynormalizationflag, kelleystagnationalpha0,
  kelleyalpha, startupflag, boxnbpoints, boxnbpointsseff, boxineqscaling,
  checkcostfunction, scalingsimplex0, guinalphamin, boxboundsalpha,
  boxtermination, boxtolf, boxnbmatch, boxkount, boxreflect, tolvarianceflag,
  tolvarianceabsolute, tolvarianceregressive, variancesimplex0, mymethod,
  myterminate, myterminateflag, greedy, output, exitflag)

  ## S3 method for class 'neldermead'
  print(x,verbose,...)

  ## S3 method for class 'neldermead'
  summary(object,showhistory,...)

  ## S3 method for class 'neldermead'
  is(x=NULL)

Arguments

optbase An object of class 'optimbase', i.e. a list created by optimbase() and containing the following elements:

  verbose The verbose option, controlling the amount of messages.
x0 The initial guess.
fx0 The value of the function for the initial guess.
xopt The optimum parameter.
fopt The optimum function value.
tolfunabsolute The absolute tolerance on function value.
tolfunrelative The relative tolerance on function value.
tolfunmethod Logical flag for the tolerance on function value in the termination criteria. This criteria is suitable for functions which minimum is associated with a function value equal to 0.
tolxabsolute The absolute tolerance on x.
tolxrelative The relative tolerance on x.
tolxmethod Possible values: FALSE, TRUE.
funevals The number of function evaluations.
maxfunevals The maximum number of function evaluations.
maxiter The maximum number of iterations.
iterations The number of iterations.
fun The cost function.
status The status of the optimization.
historyfopt The vector to store the history for fopt. The values of the cost function will be stored at each iteration in a new element, so the length of historyfopt at the end of the optimization should be the number of iterations.
historyxopt The list to store the history for xopt. The vectors of estimates will be stored on separated levels of the list, so the length of historyfopt at the end of the optimization should be the number of iterations.
verbosetermination The verbose option for termination criteria.
outputcommand The command called back for output.
outputcommandarg The outputcommand argument is initialized as a string. If the user configure this element, it is expected that a matrix of values or a list is passed so that the argument is appended to the name of the function.
numberofvariables The number of variables to optimize.
storehistory The flag which enables/disables the storing of the history.
costfargument The costf argument is initialized as a string. If the user configure this element, it is expected that a matrix of values or a list is passed so that the argument is appended to the name of the function.
boundsmin Minimum bounds for the parameters.
boundsmax Maximum bounds for the parameters.
nbineqconst The number of nonlinear inequality constraints.
logfile The name of the log file.
logfilehandle The handle for the log file.
logstartup Set to TRUE when the logging is started up.
withderivatives Set to TRUE when the method uses derivatives.
method The name of the algorithm to use.
An object of class 'simplex', i.e. a list created by `optimsimplex()`, and containing the following elements:

- **verbose**: The verbose option, controlling the amount of messages.
- **x**: The coordinates of the vertices, with size `nbve x n`.
- **n**: The dimension of the space.
- **fv**: The function values, with size `nbve x 1`.
- **nbve**: The number of vertices.

**simplexPmethod**: The method to use to compute the initial simplex.

**simplexPlength**: The length to use when the initial simplex is computed with the 'axes' or 'spendley' methods.

- **rho**: The reflection coefficient. This parameter is used when the `method` element is set to 'fixed' or 'variable'.
- **chi**: The expansion coefficient. This parameter is used when the `method` element is set to 'variable'.
- **gamma**: The contraction coefficient. This parameter is used when the `method` element is set to 'variable'.
- **sigma**: The shrinkage coefficient. This parameter is used when the `method` element is set to 'fixed' or 'variable'.

**tolfstdeviation**: The tolerance for the standard deviation.

**tolfstdeviationmethod**: Set to FALSE.

**tolsimplexizeabsolute**: The absolute tolerance on the simplex size.

**tolsimplexizerelative**: The relative tolerance on the simplex size.

**tolsimplexizemethod**: Logical flag to enable/disable the tolerance on the simplex size. When this criteria is enabled, the values of the `tolsimplexizeabsolute` and `tolsimplexizerelative` elements are used in the termination criteria. The method to compute the size is the 'sigmaplus' method.

- **simplexsize0**: Initial size of the simplex, for the tolerance on the simplex size.
- **toldeltafv**: The absolute tolerance on the difference between the highest and the lowest function values.

**tolssizedeltafvmethod**: Logical flag to enable/disable the termination criteria based on the size of the simplex and the difference of function value in the simplex. If this criteria is triggered, the status of the optimization is set to 'tolssizedeltafv'. This termination criteria uses the values of the `tolsimplexizeabsolute` and `toldeltafv` elements. This criteria is identical to Scilab's `fminsearch`.

- **historysimplex**: The list to store the history for simplex. The simplex will be stored on a new level of the list at each iteration, so the length of `historyfopt` at the end of the optimization should be the number of iterations.
coords\(0\) The coordinates of the vertices of the initial simplex. If the \texttt{simplex0method} element is set to 'given', these coordinates are used to compute the initial simplex. This matrix is expected to have shape \(n_{\text{bve}} \times n\) where \(n_{\text{bve}}\) is the number of vertices and \(n\) is the number of variables.

\texttt{simplex0deltausual}\ The relative delta for non-zero parameters in 'pfeffer' method.

\texttt{simplex0deltazero}\ The absolute delta for non-zero parameters in 'pfeffer' method.

\texttt{simplexopt}\ The optimum simplex, after one optimization process.

\texttt{restartsimplexmethod}\ The method to compute the initial simplex after a restart.

\texttt{restartmax}\ The maximum number of restarts, when automatic restart is enabled via the \texttt{restartflag} element.

\texttt{restarteps}\ The absolute epsilon value used to check for optimality in the factorial O’Neill restart detection.

\texttt{restartstep}\ The absolute step length used to check for optimality in the factorial O’Neill restart detection.

\texttt{kelleystagnationflag}\ Logical flag to enable/disable the termination criteria using Kelley’s stagnation detection, based on sufficient decrease condition. If this criteria is triggered, the status of the optimization is set to ‘kelleystagnation’.

\texttt{kelleynormalizationflag}\ Logical flag to enable/disable the normalization of the alpha coefficient in Kelley’s stagnation detection, i.e. use the value of the \texttt{kelleystagnationalpha0} element as is.

\texttt{kelleystagnationalpha0}\ The parameter used in Kelley’s stagnation detection.

\texttt{kelleyalpha}\ The current value of Kelley’s alpha, after normalization, if required.

\texttt{restartnb}\ Number of restarts performed.

\texttt{restartflag}\ Logical flag to enable/disable the automatic restart of the algorithm.

\texttt{restartdetection}\ The method to detect if the automatic restart must be performed.

\texttt{startupflag}\ Set to TRUE when the startup has been performed.

\texttt{boxnbpoints}\ The number of points in the initial simplex, when the \texttt{simplex0method} is set to 'randbounds'. The value of this element is also use to update the simplex when a restart is performed and the \texttt{restartsimplexmethod} element is set to 'randbounds'. The default value is so that the number of points is twice the number of variables of the problem.

\texttt{boxnbpointseff}\ The effective number of points required in the simplex for Box’s algorithm.

\texttt{boxineqscaling}\ The scaling coefficient used to scale the trial point for function improvement or into the constraints of Box’s algorithm.

\texttt{checkcostfunction}\ Logical flag to enable/disable the checking of the connection of the cost function.
The algorithm used to scale the initial simplex into the nonlinear constraints. The following two algorithms are provided:

- 'tox0' scales the vertices toward the initial guess.
- 'tocentroid' scales the vertices toward the centroid, as recommended by Box.

If the centroid happens to be unfeasible, because the constraints are not convex, the scaling of the initial simplex toward the centroid may fail. Since the initial guess is always feasible, scaling toward the initial guess cannot fail.

The minimum value of alpha when scaling the vertices of the simplex into nonlinear constraints in Box’s algorithm.

The parameter used to project the vertices into the bounds in Box’s algorithm.

Logical flag to enable/disable Box’s termination criteria.

The absolute tolerance on difference of function values in the simplex, suggested by Box. This tolerance is used if the boxtermination element is set to TRUE.

The number of consecutive match of Box’s termination criteria.

Current number of consecutive match.

The reflection factor in Box’s algorithm.

Logical flag to enable/disable the termination criteria based on the variance of the function value. If this criteria is triggered, the status of the optimization is set to 'tolvariance'. This criteria is suggested by Nelder and Mead.

The absolute tolerance on the variance of the function values of the simplex.

The relative tolerance on the variance of the function values of the simplex.

Relative tolerance on variance.

A user-derined simplex algorithm.

A user-defined terminate function.

Logical flag to enable/disable the user-defined terminate function.

Logical flag to enable/disable greedy Nelder-Mead.

The command to call back for user-defined output of specialized function.

Logical flag to enable/disable the user-defined output of specialized function.

An object of class 'neldermead'.

A logical flag, controlling the amount of data printed.

optional arguments to 'print' or 'plot' methods.

An object of class 'neldermead'.

Optional logical flag, to define whether optimization history must be summarized or not.
The `neldermead` function returns a new object of class 'neldermead', with the following default content:

**optbase**  An object of class 'optimbase' with the following default content:

- **verbose**  Default is FALSE.
- **x0**  Default is NULL.
- **fx0**  Default is NULL.
- **xopt**  Default is 0.
- **fopt**  Default is 0.
- **tolfunabsolute**  Default is 0.
- **tolfunrelative**  Default is .Machine$double.eps.
- **tolfunmethod**  Default is FALSE.
- **tolxabsolute**  Default is 0.
- **tolxrelative**  Default is .Machine$double.eps.
- **tolxmethod**  Default is TRUE.
- **funevals**  Default is 0.
- **maxfunevals**  Default is 100.
- **maxiter**  Default is 100.
- **iterations**  Default is 0.
- **fun**  Default is ".
- **status**  Default is ".
- **historyfopt**  Default is NULL.
- **historyxopt**  Default is NULL.
- **verbosetermination**  Default is FALSE.
- **outputcommand**  Default is ".
- **outputcommandarg**  Default is ". If the user configures this element, it is expected to be an object of class 'optimbase.outputargs' or will be coerced to an object of class 'optimbase.outputargs'.
- **numberofvariables**  Default is 0.
- **storehistory**  Default is FALSE.
- **costfargument**  Default is ".
- **costfargument**  If the user configures this element, it is expected to be an object of class 'optimbase.functionargs' or will be coerced to an object of class 'optimbase.functionargs'.
- **boundsmin**  Default is NULL.
- **boundsmax**  Default is NULL.
- **nbineqconst**  Default is 0.
- **logfile**  Default is ".
- **logfilehandle**  Default is 0.
- **logstartup**  Default is FALSE.
- **withderivatives**  Default is FALSE.
- **method**  Default is 'variable'.
- **simplex0**  Default is an object of class 'simplex', with the following content:
verbose  Default is 0.
  x  Default is NULL.
  n  Default is 0.
  fv  Default is NULL.
  nbve  Default is 0.

simplex0method  Default is 'axes'.
simplex0length  Default is 1.
rho  Default is 1.
chi  Default is 2.
gamma  Default is 0.5.
sigma  Default is 0.5.
tolfstdeviation  Default is 0.
tolfstdeviationmethod  Default is FALSE.
tolsimplexizeabsolute  Default is 0.
tolsimplexizerelative  Default is .Machine$double.eps.
tolsimplexizemethod  Default is FALSE.
simplexsize0  Default is 0.
toldeltafv  Default is .Machine$double.eps.
tolssizedeltafvmethod  Default is FALSE.
historysimplex  Default is NULL.
coords0  Default is NULL.
simplex0deltausual  Default is 0.05.
simplex0deltazero  Default is 0.0075.
simplexopt  Default is NULL.
restartsimplexmethod  Default is 'oriented'.
restartmax  Default is 3.
restarteps  Default is .Machine$double.eps.
restartstep  Default is 1.
kelleystagnationflag  Default is FALSE.
kelleynormalizationflag  Default is TRUE, i.e. the simplex gradient of the initial simplex is taken into account in the stagnation detection.
kelleystagnationalpha0  Default is 1.e-4.
kellyalpha  Default is 1.e-4.
restartnb  Default is 0.
restartflag  Default is FALSE.
restartdetection  Default is 'oneill'.
startupflag  Default is FALSE.
boxnbpoints  Default is '2n'.

boxnbpoints  Default is '2n'.
boxnbpointseff  Default is 0.
boxineqscaling  Default is 0.
checkcostfunction  Default is TRUE.
scalingsimplex0  Default is 'tox0'.
guinalphamin  Default is 1.e-6.
boxtermination  Default is FALSE.
boxtolf  Default is 1.e-5.
boxnbmatch  Default is 5.
boxkount  Default is 0.
boxreflect  Default is 1.3.
tolvarianceflag  Default is FALSE.
tolabsolvariance  Default is 0.
tolrelativevariance  Default is .Machine$double.eps.
variancesimplex0  Default is .Machine$double.eps.
mymethod  Default is NULL.
myterminate  Default is NULL.
myterminateflag  Default is FALSE.
greedy  Default is FALSE.
output  Default is list().
extiflag  Default is FALSE.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

optimbase, optimsimplex

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neldermead.algo  \textit{Nelder-Mead Algorithm}

Description

\texttt{neldermead.algo} performs an optimization without restart using the method associated with the \texttt{method} element of the \texttt{neldermead} object; \texttt{neldermead.fixed}, \texttt{neldermead.variable}, \texttt{neldermead.box}, \texttt{boxlinesearch}, \texttt{neldermead.storehistory}, \texttt{neldermead.termination}, and \texttt{neldermead.interpolate} are utility functions for \texttt{neldermead.algo}. 
Usage

neldermead.algo(this = NULL)
neldermead.fixed(this = NULL)
neldermead.variable(this = NULL)
neldermead.box(this = this)
boxlinesearch(this = NULL, n = NULL, xbar = NULL, xhigh = NULL, fhigh = NULL, rho = NULL)
neldermead.storehistory(this = NULL, n = NULL, fopt = NULL, xopt = NULL, fv = NULL, xcoords = NULL)
neldermead.termination(this = NULL, fvinitial = NULL, oldfvmean = NULL, newfvmean = NULL, previousxopt = NULL, currentxopt = NULL, simplex = NULL)
neldermead.interpolate(x1 = NULL, x2 = NULL, fac = NULL)

Arguments

this A neldermead object.
n Number of variables.
xbar The centroid.
xhigh The high point.
fhigh The value of the cost function at xhigh.
rho The reflection factor.
fopt The current value of the function at the current optimum point estimate.
xopt The current optimum point estimate.
fv The function values, with size nbve x 1.
xcoords Matrix of size n x n+1, coordinates of the n+1 vertices
fvinitial The initial cost function value.
oldfvmean The old cost function value average on the simplex.
ewfvmean The new cost function value average on the simplex.
previousxopt The previous point estimate.
currentxopt The current point estimate.
simplex The simplex. The best point estimate in the simplex is expected to be stored at 1, while the worst point estimate in the simplex is expected to be stored at n+1.
x1 The first reference point estimate to perform the interpolation.
x2 The second reference point estimate to perform the interpolation.
fac A factor to perform the interpolation.

Details

neldermead.fixed The simplex algorithm with fixed size simplex. We implement the following 'rules' of the method of Spendley et al.

- Rule 1 is strictly applied, but the reflection is done by reflection of the high point, since we minimize a function instead of maximizing it, like Spendley.
• Rule 2 is NOT implemented, as we expect that the function evaluation is not subject to errors.
• Rule 3 is applied, i.e. reflection with respect to next to high point. A shrink step is included, with shrinkage factor sigma.

Rule 1. Ascertain the lowest reading \( y \), of \( y_1 \ldots y_{k+1} \) Complete a new simplex \( S_p \) by excluding the point \( V_p \) corresponding to \( y \), and replacing it by \( V^* \) defined as above.

Rule 2. If a result has occurred in \((k + 1)\) successive simplexes, and is not then eliminated by application of Rule 1, do not move in the direction indicated by Rule 1, or at all, but discard the result and replace it by a new observation at the same point.

Rule 3. If \( y \) is the lowest reading in \( S_0 \), and if the next observation made, \( y^* \), is the lowest reading in the new simplex \( S \), do not apply Rule 1 and return to \( S_0 \) from \( S_p \). Move out of \( S \), by rejecting the second lowest reading (which is also the second lowest reading in \( S_0 \)).

neldermead variable The original Nelder-Mead algorithm, with variable-size simplex.
neldermead box The Nelder-Mead algorithm, with variable-size simplex and modifications by Box for bounds and inequality constraints.
boxlinesearch Called by neldermead.box, i.e. Box's method. Perform a line search from \( x_{bar} \), on the line \((x_{high}, x_{bar})\). The reflected point estimate satisfies the following constraints:
   • \( f_r < f_{high} \)
   • \( x_r \) satisfies the bounds constraints
   • \( x_r \) satisfies the nonlinear positive inequality constraints
   • \( x_r \) satisfies the linear positive inequality constraints

The method is based on projection and scaling toward the centroid.
neldermead storehistory Store the optimization history into the neldermead object.
neldermead termination Determine if the algorithm must continue or terminate. The function uses the cost function average in the simplex instead of the best cost function value. This is because the function average changes at each iteration. Instead, the best function value has a step-by-step evolution and may not change between two successive iterations, leading to a stop of the algorithm.
neldermead interpolate Compute the point estimate \( x_i \) as an interpolation between \( x_1 \) and \( x_2 \), as follows: \( x_i = (1+\text{fac})x_1 - \text{fac}x_2 \)

Value

neldermead fixed, neldermead variable, and neldermead box Return the updated neldermead object, containing the optimum point estimate.
boxlinesearch Return a list with the following elements:
   • \textthis The updated neldermead object.
   • \textstatus TRUE if the search is successful, FALSE otherwise.
   • \txr The reflected point estimate.
   • \tf \text The value of the cost function at \txr.
neldermead storehistory Return the updated neldermead object.
neldermead termination Return a list with the following elements:
   • \textthis The updated neldermead object
**terminate**  TRUE if the algorithm terminates, FALSE if the algorithm must continue.

**status**  The termination status: 'continue', 'maxiter', 'maxfuneval', 'tolf', 'tolx', 'tolsize', 'tolsizedeltafv', 'kelleystagnation', 'tolboxf', 'tolvariance' or the user-defined termination status.

**neldermead.interpoltate**  Return a new point estimate, i.e. a column vector.

**Author(s)**

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

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**neldermead.destroy**  Erase a neldermead object.

**Description**

**neldermead.destroy** calls **optimbase.destroy** and **optimsimplex.destroy** to erase the content of this$optbase$ and this$simplex$.

**Usage**

```
neldermead.destroy(this = NULL)
```

**Arguments**

**this**  A neldermead object.

**Value**

Return an updated neldermead object.

**Author(s)**

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)

Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

**See Also**

*optimbase.destroy*, *optimsimplex.destroy*
neldermead.function  Call Cost Function.

Description
Simple way to compute the value of the cost function specified in a neldermead object.

Usage
neldermead.function(this = NULL, x = NULL)

Arguments
- this: A neldermead object.
- x: The point estimate where the cost function is to be evaluated.

Value
Returns the value of the cost function.

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

neldermead.get  Get the value for the given element

Description
Get the value for the given element in a neldermead object.

Usage
neldermead.get(this = NULL, key = NULL)

Arguments
- this: A neldermead object.
- key: The name of the key to query.

Value
Return the value of the list element key, or an error message if key does not exist in the neldermead object this.
neldermead.restart

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

neldermead.set, optimbase.get

neldermead.restart  Restart neldermead search.

Description

Update the simplex with neldermead.updatesimp and restart the search with neldermead.search.

Usage

neldermead.restart(this = NULL)

Arguments

this  A neldermead object.

Value

Returns an updated neldermead object.

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

neldermead.updatesimp, neldermead.search,
neldermead.search  

Starts the optimization

Description
Perform the optimization associated with the method associated with the method element of the neldermead object and find the optimum. If the restartflag element is enabled, automatic restarts are performed, based on the restartdetection element.

Usage
neldermead.search(this = NULL)

Arguments
this  
A neldermead object.

Value
Return an updated neldermead object.

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also
fminsearch, neldermead, neldermead.set.

neldermead.set  Neldermead Object Configuration

Description
Configure the current neldermead object with the given value for the given key.

Usage
neldermead.set(this = NULL, key = NULL, value = NULL)

Arguments
this  
The current neldermead object.
key  
The key to configure. See details for the list of possible keys.
value  
The value to assign to the key.
Details

neldermead.set sets the content of the key element of the neldermead object this to value. If key is a sub-element of this@optbase, value is assigned by optimbase.set.

The main available keys are the following:

’-verbose’ Set to 1 to enable verbose logging.
’-verbosetermination’ Set to 1 to enable verbose termination logging.
’-x0’ The initial guess, as a n x 1 column vector, where n is the number of variables.
’-maxfunevals’ The maximum number of function evaluations. If this criteria is triggered during optimization, the status of the optimization is set to ’maxfuneval’.
’-maxiter’ The maximum number of iterations. If this criteria is triggered during optimization, the status of the optimization is set to ’maxiter’.
’-tolfunabsolute’ The absolute tolerance for the function value.
’-tolfunrelative’ The relative tolerance for the function value.
’-tolfunmethod’ The method used for the tolerance on function value in the termination criteria. The following values are available: TRUE, FALSE. If this criteria is triggered during optimization, the status of the optimization is set to ’tolf’.
’-tolxabsolute’ The absolute tolerance on x.
’-tolxrelative’ The relative tolerance on x.
’-tolxmethod’ The method used for the tolerance on x in the termination criteria. The following values are available: TRUE, FALSE. If this criteria is triggered during optimization, the status of the optimization is set to ’tolx’.
’-function’ The objective function, which computes the value of the cost and the non linear constraints, if any. See vignette(‘neldermead’,package=’neldermead’) for the details of the communication between the optimization system and the cost function.
’-costfargument’ An additional argument, passed to the cost function.
’-outputcommand’ A command which is called back for output. See vignette(‘neldermead’,package=’neldermead’) for the details of the communication between the optimization system and the output command function.
’-outputcommandarg’ An additional argument, passed to the output command.
’-numberofvariables’ The number of variables to optimize.
’-storehistory’ Set to TRUE to enable the history storing.
’-boundsmin’ The minimum bounds for the parameters.
’-boundsmax’ The maximum bounds for the parameters.
’-nbineqconst’ The number of inequality constraints.
’-method’ The name of the algorithm to use. The following methods are available:
   ’fixed’ the fixed simplex shape algorithm of Spendley et al. This algorithm is for unconstrained problems (i.e. bounds and non linear constraints are not taken into account)
   ’variable’ the variable simplex shape algorithm of Nelder and Mead. This algorithm is for unconstrained problems (i.e. bounds and non linear constraints are not taken into account)
   ’box’ Box’s complex algorithm. This algorithm takes into account bounds and nonlinear inequality constraints.
'mine' the user-defined algorithm, associated with the mymethod element. See vignette('neldermead', package='neldermead') for details.

'-simplex0method' The method to use to compute the initial simplex. The first vertex in the simplex is always the initial guess associated with the x0 element. The following methods are available:

'given' The coordinates associated with the coords0 element are used to compute the initial simplex, with arbitrary number of vertices. This allows the user to setup the initial simplex by a specific method which is not provided by the current package (for example with a simplex computed from a design of experiments). This allows also to configure the initial simplex so that a specific behaviour of the algorithm is to be reproduced (for example the Mac Kinnon test case). The given matrix is expected to have nbve rows and n columns, where n is the dimension of the problem and nbve is the number of vertices.

'axes' The simplex is computed from the coordinate axes and the length associated with the simplex0length element.

'spendley' The simplex is computed so that it is regular with the length associated with the simplex0length element (i.e. all the edges have the same length).

'pfeffer' The simplex is computed from an heuristic, in the neighborhood of the initial guess. This initial simplex depends on the -simplex0deltausual and -simplex0deltazero.

'randbounds' The simplex is computed from the bounds and a random number. This option is available only if bounds are available: if bounds are not available, an error is generated. This method is usually associated with Box’s algorithm. The number of vertices in the simplex is taken from the boxnbpoints element.

'-coords0' The coordinates of the vertices of the initial simplex. If the simplex0method element is set to 'given', these coordinates are used to compute the initial simplex. This matrix is expected to have shape nbve x n, where nbve is the number of vertices and n is the number of variables.

'-simplex0length' The length to use when the initial simplex is computed with the 'axes' or 'spendley' methods. If the initial simplex is computed from 'spendley' method, the length is expected to be a scalar value. If the initial simplex is computed from 'axes' method, it may be either a scalar value or a vector of values, of length n, where n is the number of variables.

'-simplex0deltausual' The relative delta for non-zero parameters in 'pfeffer' method.

'-simplex0deltazero' The absolute delta for non-zero parameters in 'pfeffer' method.

'-rho' The reflection coefficient. This parameter is used when the method element is set to 'fixed' or 'variable'.

'-chi' The expansion coefficient. This parameter is used when the method element is set to 'variable'.

'-gamma' The contraction coefficient. This parameter is used when the method element is set to 'variable'.

'-sigma' The shrinkage coefficient. This parameter is used when the method element is set to 'fixed' or 'variable'.

'-tolsimplexizemethod' Set to FALSE to disable the tolerance on the simplex size. If this criteria is triggered, the status of the optimization is set to 'tolsize'. When this criteria is enabled, the values of the tolsimplexizeabsolute and tolsimplexizerelative elements are used in the termination criteria. The method to compute the size is the 'sigmaplus' method.
'-tolsimplexizeabsolute'  The absolute tolerance on the simplex size.
'-tolsimplexizerelative'  The relative tolerance on the simplex size.
'-tolsizedeltafvmethod'  Set to TRUE to enable the termination criteria based on the size of the simplex and the difference of function value in the simplex. If this criteria is triggered, the status of the optimization is set to 'tolsizedeltafv'. This termination criteria uses the values of the tolsimplexizeabsolute and toldeltafv elements.
'-toldeltafv'  The absolute tolerance on the difference between the highest and the lowest function values.
'-tolvarianceflag'  Set to TRUE to enable the termination criteria based on the variance of the function value. If this criteria is triggered, the status of the optimization is set to 'tolvariance'. This criteria is suggested by Nelder and Mead.
'-tolabsolutevariance'  The absolute tolerance on the variance of the function values of the simplex.
'-tolrelativevariance'  The relative tolerance on the variance of the function values of the simplex.
'-kelleystagnationflag'  Set to TRUE to enable the termination criteria using Kelley's stagnation detection, based on sufficient decrease condition. If this criteria is triggered, the status of the optimization is set to 'kelleystagnation'.
'-kelleynormalizationflag'  Set to FALSE to disable the normalization of the alpha coefficient in Kelley’s stagnation detection, i.e. use the value of the kelleystagnationalpha0 element as is. Default value is TRUE, i.e. the simplex gradient of the initial simplex is taken into account in the stagnation detection.
'-kelleystagnationalpha0'  The parameter used in Kelley’s stagnation detection.
'-restartflag'  Set to TRUE to enable the automatic restart of the algorithm.
'-restartdetection'  The method to detect if the automatic restart must be performed. The following methods are available:
    'oneill'  The factorial local optimality test by O’Neill is used. If the test finds a local point which is better than the computed optimum, a restart is performed.
    'kelley'  The sufficient decrease condition by O’Neill is used. If the test finds that the status of the optimization is ‘kelleystagnation’, a restart is performed. This status may be generated if the -kelleystagnationflag option is set to TRUE.
'-restartmax'  The maximum number of restarts, when automatic restart is enabled via the -restartflag option.
'-restarteps'  The absolute epsilon value used to check for optimality in the factorial O’Neill restart detection.
'-restartstep'  The absolute step length used to check for optimality in the factorial O’Neill restart detection.
'-restartsimplexmethod'  The method to compute the initial simplex after a restart. The following methods are available:
    'given'  The coordinates associated with the coords element are used to compute the initial simplex, with arbitrary number of vertices. This allow the user to setup the initial simplex by a specific method which is not provided by the current package (for example with a simplex computed from a design of experiments). This allows also to configure the initial simplex so that a specific behaviour of the algorithm is to be reproduced (for example the McKinnon test case). The given matrix is expected to have nbve rows and n columns, where n is the dimension of the problem and nbve is the number of vertices.
'axes' The simplex is computed from the coordinate axes and the length associated with the
-simplex0length option.

'spendley' The simplex is computed so that it is regular with the length associated with the
-simplex0length option (i.e. all the edges have the same length).

'pfeffer' The simplex is computed from an heuristic, in the neighborhood of the initial guess.
This initial simplex depends on the -simplex0deltausual and -simplex0deltazero.

'randbounds' The simplex is computed from the bounds and a random number. This option
is available only if bounds are available; if bounds are not available, an error is generated.
This method is usually associated with Box's algorithm. The number of vertices in the
simplex is taken from the -boxnbpoints option.

'oriented' The simplex is computed so that it is oriented, as suggested by Kelley.

'-scalingsimplex0' The algorithm used to scale the initial simplex into the nonlinear constraints.
The following two algorithms are provided:

'tox0' scales the vertices toward the initial guess.
'tocentroid' scales the vertices toward the centroid, as recommended by Box.

If the centroid happens to be unfeasible, because the constraints are not convex, the scaling
of the initial simplex toward the centroid may fail. Since the initial guess is always feasible,
scaling toward the initial guess cannot fail.

'-boxnbpoints' The number of points in the initial simplex, when the -simplex0method is set to
'randbounds'. The value of this option is also used to update the simplex when a restart is
performed and the -restartsimplexmethod option is set to 'randbounds'. The default value is
so that the number of points is twice the number of variables of the problem.

'-boxineqscaling' The scaling coefficient used to scale the trial point for function improvement or
into the constraints of Box's algorithm.

'-guinalphamin' The minimum value of alpha when scaling the vertices of the simplex into non-
linear constraints in Box's algorithm.

'-boxreflect' The reflection factor in Box's algorithm.

'-boxtermination' Set to TRUE to enable Box's termination criteria.

'-boxtolf' The absolute tolerance on difference of function values in the simplex, suggested by
Box. This tolerance is used if the -boxtermination element is set to TRUE.

'-boxnbmatch' The number of consecutive match of Box's termination criteria.

'-boxboundsalpha' The parameter used to project the vertices into the bounds in Box's algorithm.

'-mymethod' A user-defined simplex algorithm. See vignette('neldermead',package='neldermead')
for details.

'-myterminate' A user-defined terminate function. See vignette('neldermead',package='neldermead')
for details.

'-myterminateflag' Set to TRUE to enable the user-defined terminate function.

Value
An updated neldermead object.
optimget

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also
neldermead

optimget Queries an optimization option list

Description
This function allows to make queries on an existing optimization option list. This list must have been created and updated by the optimset function. The optimget allows to retrieve the value associated with a given key.

Usage
optimget(options = NULL, key = NULL, value = NULL)

Arguments
options A list created or modifies by optimset.
key A single character string, which should be the name of the field in options to query (case insensitive).
value A default value.

Details
key is matched against the field names of options using grep and a case-insensitive regular expression. If key is not found in options, the function returns NULL. If several matches are found, optimget is stopped.

Value
Return options$key if key is found in options. Return value, otherwise.

Author(s)
Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also
optimset
**Examples**

```r
opt <- optimset(method='fminsearch')
optimget(opt,'Display')
optimget(opt,'abc','@')
```

---

**optimset**  
*Configures and returns an optimization data structure.*

**Description**

This function creates or updates a list which can be used to modify the behaviour of optimization methods. The goal of this function is to manage the options list with a set of fields (for example, 'MaxFunEvals', 'MaxIter', etc...). The user can create a new list with empty fields or create a new structure with default fields which correspond to a particular algorithm. The user can also configure each field and set it to a particular value. Finally, the user passes the list to an optimization function so that the algorithm uses the options configured by the user.

**Usage**

```r
optimset(method = NULL,...)
```

**Arguments**

- **method**  
  If provided, the method calls the `optimset.method` function. If the content of method is recognized, a default set of options are returned. The only current recognized character strings are 'fminsearch' and 'fminbnd'.

- **...**  
  Additional arguments which would be included in the options output if the method argument is not used. See Details.

**Details**

Most optimization algorithms require many algorithmic parameters such as the number of iterations or the number of function evaluations. If these parameters are given to the optimization function as input parameters, this forces both the user and the developer to manage many input parameters. The goal of the `optimset` function is to simplify the management of input arguments, by gathering all the parameters into a single list.

While the current implementation of the `optimset` function only supports the `fminsearch` and `fminbnd` function, it is designed to be extended to as many optimization function as required. Because all optimization algorithms do not require the same parameters, the data structure aims at remaining flexible. But, most of the time, most parameters are the same from algorithm to algorithm, for example, the tolerance parameters which drive the termination criteria are often the same, even if the termination criteria itself is not the same.

Optimization parameters that are returned by the `optimset` function and that can be defined in ... are the following:

- **Display**  
  The verbose level. The default value is 'notify'. The following is a list of available verbose levels.
optimset

'off' The algorithm displays no message at all.

'notify' The algorithm displays message if the termination criteria is not reached at the end of the optimization. This may happen if the maximum number or iterations of the maximum number of function evaluations is reached and warns the user of a convergence problem.

'final' The algorithm displays a message at the end of the optimization, showing the number of iterations, the number of function evaluations and the status of the optimization. This option includes the messages generated by the 'notify' option i.e. warns in case of a convergence problem.

'iter' The algorithm displays a one-line message at each iteration. This option includes the messages generated by the 'notify' option i.e. warns in case of a convergence problem. It also includes the message generated by the 'final' option.

FunValCheck A logical flag to enable the checking of function values.

MaxFunEvals The maximum number of evaluations of the cost function.

MaxIter The maximum number of iterations.

OutputFcn A function which is called at each iteration to print out intermediate state of the optimization algorithm (for example into a log file).

PlotFcns A function which is called at each iteration to plot the intermediate state of the optimization algorithm (for example into a 2D graphic).

TolFun The absolute tolerance on function value.

TolX The absolute tolerance on the variable x.

nbMatch Specific to Box method: the number of consecutive times the TolFun criteria must be met to terminate the optimization.

boundsAlpha Specific to Box method: the parameter used to project the vertices into the bounds in Box’s algorithm

boxScaling Specific to Box method: the scaling coefficient used to scale the trial point for function improvement or into the constraints of Box’s algorithm

alphaMin Specific to Box method: the minimum value of alpha when scaling the vertices of the simplex into nonlinear constraints in Box’s algorithm

Output and plot functions The 'OutputFcn' and 'PlotFcns' options accept as argument a function (or a list of functions). In the client optimization algorithm, this output or plot function is called back once per iteration. It can be used by the user to display a message in the console, write into a file, etc... The output or plot function is expected to have the following definition:

myfun <- function(x, optimValues, state)

where the input parameters are:

x The current point estimate.

optimValues A list which contains the following fields:

  funccount The number of function evaluations.
  fval The best function value.
  iteration The current iteration number.
  procedure The type of step performed. This string depends on the specific algorithm (see fminsearch for details).
**state** the state of the algorithm. The following states are available:
- 'init' when the algorithm is initializing,
- 'iter' when the algorithm is performing iterations,
- 'done' when the algorithm is terminated.

**Value**

Return a list with the following fields: Display, FunValCheck, MaxFunEvals, MaxIter, OutputFcn, PlotFcns, TolFun, TolX, nbMatch, boundsAlpha, boxScaling, and alphaMin.

**Author(s)**

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

optimset.method, fminsearch, fminbnd

**Examples**

```latex
optimset()
optimset(Display='iter')
optimset(method='fminbnd')
```

**Description**

This function returns a default set of optimization options for defined 'methods'; optimset.method is called by optimset when a method was provided as input. Currently, the only valid method is 'fminsearch'.

**Usage**

```latex
optimset.method(method = NULL)
```

**Arguments**

- **method** A character string.

**Value**

Returns a list with the following fields: Display, FunValCheck, MaxFunEvals, MaxIter, OutputFcn, PlotFcns, TolFun, and TolX.
Secondary search functions

Author(s)

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
Author of R adaptation: Sebastien Bihorel (<sb.pmlab@gmail.com>)

See Also

optimset

Examples

optimset.method('fminsearch')
## Not run: optimset.method('abc')

Description

Utility functions for neldermead.search and dependent functions.

Usage

neldermead.startup(this = NULL)
neldermead.log(this = NULL, msg = NULL)
neldermead.scaletox0(this = NULL, simplex0 = NULL)
neldermead.scaletocenter(this = NULL, simplex0 = NULL, xo = NULL)
neldermead.termdstartup(this = NULL)
neldermead.outputcmd(this = NULL, state = NULL, simplex = NULL, step = NULL)
neldermead.autorestart(this = NULL)
neldermead.istorestart(this = NULL)
neldermead.isroneill(this = NULL)
neldermead.isrkelley(this = this)
neldermead.updatesimp(this = NULL)
scaleinconstraints(this = NULL, x = NULL, xref = NULL)
neldermead.costf(x = NULL, this = NULL)

Arguments

this A neldermead object.
msg A character string.
simplex0 The initial simplex object.
x0 A column matrix of initial parameters.
state The state of the algorithm, either 'init', 'done' or 'iter'.
simplex The current simplex object.
Secondary search functions

step The type of step performed during the iteration: 'init', 'done', 'reflection', 'expansion', 'insidecontraction', 'outsidecontraction', 'reflectionnext' or 'shrink'.
x The point estimate to scale.
xref The reference point estimate.

Details

neldermead.startup Startup the algorithm. Compute the initial simplex, depending on the content of the simplexmethod element of the neldermead object ('given', 'axes', 'spendley', 'pfeffer' or 'randbounds').
neldermead.log Print a message to the log file using optimbase.log.
neldermead.scaletox Scale the simplex into the nonlinear inequality constraints, if any. Scale toward x0, which is feasible.
neldermead.scaletocenter Scale the simplex into the nonlinear inequality constraints, if any. Scale to the centroid of the points which satisfy the constraints. This is Box's method for scaling. It is unsure, since the centroid of the points which satisfy the constraints may not be feasible.
neldermead.termstartup Initialize Kelley’s stagnation detection system when normalization is required, by computing kelleyalpha. If the simplex gradient is zero, then use alpha0 as alpha.
neldermead.outputcmd Call the array of user-defined output functions

neldermead.autorestart Perform an optimization with automatic restart. The loop processes for i = 1 to restartmax + 1. This is because a RE-start is performed after one simulation has been performed, hence the 'RE'.
neldermead.istorestart Determine if the optimization is to restart using neldermead.isroneill or neldermead.isrkelley depending on the content of the restartdetection element.
neldermead.isroneill Determine if the optimization is to restart. Use O’Neill method as a criteria for restart. It is an axis-by-axis search for optimality.
neldermead.isrkelley Determine if the optimization is to restart. Use kelleystagnation as a criteria for restart.
neldermead.updatesimp Update the initial simplex simplex0 for a restart.
scaleinconstraints Given a point reference to scale and a reference point which satisfies the constraints, scale the point towards the reference point estimate until it satisfies all the constraints.
neldermead.costf Call the cost function and return the value. This function is given to the simplex function class as a callback. Input/Output arguments are swapped w.r.t. optimbase.function, so that it matches the requirements of simplex methods.

Value

neldermead.startup Return an updated neldermead object this.
neldermead.log Return the neldermead object this.
neldermead.scaletox Return an updated simplex.
neldermead.scaletocenter Return an updated simplex.
**Secondary search functions**

neldermead.termstartup Return an updated neldermead object this.
neldermead.outputcmd Do not return any data, but execute the output function(s).
neldermead.autorestart Return an updated neldermead object this.
neldermead.istorestart Return a list with the following elements:
  - **this** The input neldermead object.
  - **istorestart** Set to TRUE if the optimization is to restart, to FALSE otherwise.
neldermead.isroneill Return a list with the following elements:
  - **this** The input neldermead object.
  - **istorestart** Set to TRUE if the optimization is to restart, to FALSE otherwise.
neldermead.isrkelley Return a list with the following elements:
  - **this** The input neldermead object.
  - **istorestart** Set to TRUE if the optimization is to restart, to FALSE otherwise.
neldermead.updatesimp Return an updated neldermead object this.
scaleinconstraints Return a list with the following elements:
  - **this** The updated neldermead object.
  - **isscaled** TRUE if the procedure has succeeded before boxnb1loops, FALSE if it has failed.
  - **p** The scaled parameters.
neldermead.costf Return a list with the following elements:
  - **f** The value of the cost function.
  - **this** The updated neldermead object.

**Author(s)**

Author of Scilab neldermead module: Michael Baudin (INRIA - Digiteo)
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